

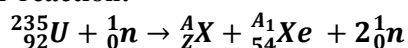
Exam in Chemistry 1

Exercise 1: (3 pts)

I. Let ${}^{A_1}_{54}\text{Xe}$ be a chemical element.

1. Give its nuclear composition.
2. Calculate the binding energy per nucleon in MeV/nucleon.

II. Consider the following nuclear reaction:



1. Balance this nuclear reaction and specify its type.
2. This reaction releases an energy of -2.955×10^{-11} J. Calculate the atomic mass of the element ${}^A_Z\text{X}$.

III. The atomic mass of natural uranium is 238.039 g/mol and it has two isotopes: ${}^{238}_{92}\text{U}$, ${}^{235}_{92}\text{U}$. The natural abundances of these isotopes are $X_1\%$, $X_2\%$, respectively. Calculate the abundances of these two isotopes.

Element	Proton	Neutron	A ₁ Xe	²³⁸ ₉₂ U	²³⁵ ₉₂ U	C = 3.10 ⁸ m/s
Mass in U	1.00727	1.00866	139.89	238.0505	235.044	

Exercise 2: (4.75 pts)

I- We consider the Paschen series of the emission spectrum of the hydrogen atom:

1. Which transition corresponds to the spectral line of frequency $\nu = 23.36 \times 10^{13}$ Hz?
2. Calculate the energy corresponding to this transition using two methods.
3. The wavelength corresponding to the second line of the Balmer series is $\lambda_1 = 486$ nm. Calculate, in terms of λ_1 , the wavelength λ_2 corresponding to the third line of the Paschen series.

II- For a hydrogen-like ion, the same electronic transition studied in Part I corresponds to a frequency $\nu_1 = 210.29 \times 10^{13}$ Hz.

1. Determine Z for this hydrogen-like ion.
2. Calculate the energy required to ionize this hydrogen-like ion starting from $n = 5$.

$$h = 6.62 \cdot 10^{-34} \text{ J.s}, R_H = 1.1 \cdot 10^7 \text{ m}^{-1}; C = 3.10^8 \text{ m/s}$$

Exercise 3: (6.25 pts)

Let the following elements be given: ${}_{16}\text{S}$, ${}_{48}\text{Cd}$, ${}_{37}\text{Rb}$

1. Write the abbreviated electron configuration using noble gas notation for each element in the ground state, then determine for each element: period, group, and column (summarize your answer in a table).
2. The elements ${}_{17}\text{Cl}$, ${}_{16}\text{S}$, ${}_{15}\text{P}$ belong to the same period. Arrange them in increasing order of atomic radius and justify your answer.
3. Determine the electronic configuration and atomic number of an element X that has 5 electrons in the outermost subshell defined by $\ell = 1$ and $n = 4$ in the ground state. Is X a metallic element or not?
4. Using Slater's rules, calculate the first and second ionization energies of the atom ${}_{2}\text{He}$.

The studied electron l	Electrons j that screen i						
	1s	2s2p	3s3p	3d	4s4p	4d	4f
1s	0.31	0	0	0	0	0	0
2s2p	0.85	0.35	0	0	0	0	0
3s3p	1	0.85	0.35	0	0	0	0
3d	1	1	1	0.35	0	0	0
4s4p	1	1	0.85	0.85	0.35	0	0

Exercise 4: (6 pts)

- 1- Give the Lewis structures of the compounds PCl_3 ; HPBe ; NH_4^+ .
- 2- Does the compound PCl_3 have a dipole moment
- 3- If yes, indicate the partial charges on the atoms and the direction of the dipole moment for each bond.
- 4- What is the type of bond between the elements P and Cl?
 $\text{P} (Z=15, \kappa=2.1)$; $\text{Cl} (Z=17, \kappa=3.1)$; $\text{H} (Z=1)$; $\text{Be} (Z=4)$; $\text{N} (Z=7)$

The model correction for the exam (chemistry 1 : 2025-2026)

Exercise 1:

I-

1- Nuclear composition

We consider the nucleus of xenon: ${}^{140}_{54}\text{Xe}$.

Number of protons $Z = 54$.

Number of neutrons $N = A - Z = 140 - 54 = 86$.

2- The Binding energy per nucleon:

$$\frac{E_b}{A} = \frac{\Delta m c^2}{A} = \frac{[Z m_p + N m_n - m(\text{Xe})] \times c^2}{A}$$

$$\frac{E_b}{A} = \frac{(54 \times 1.00727 + 86 \times 1.00866 - 139.89) \times 931.5}{140} = 8.31 \text{ MeV/nucleon}$$

II-

1- ${}^{235}_{92}\text{U} + {}^1_0\text{n} \rightarrow {}^{94}_{38}\text{X} + {}^{140}_{54}\text{Xe} + 2{}^1_0\text{n}$

This is a nuclear fission reaction.

2- The atomic mass of the element ${}^A_Z\text{X}$.

$$\Delta E = \frac{-2.955 \times 10^{-11}}{1.6 \times 10^{-13}} = -184.68 \text{ Mev}$$

$$\Delta E = \Delta m \cdot c^2 = \Delta m \cdot 931.5$$

$$\Rightarrow \Delta m = \frac{\Delta E}{931.5} = -0.1982u$$

$$\Delta m = (m_f - m_i) = m_{{}^{94}_{38}\text{X}} + m_{{}^{140}_{54}\text{Xe}} + m_{{}^1_0\text{n}} - m_{{}^{235}_{92}\text{U}}$$

$$\Rightarrow m_{{}^{94}_{38}\text{X}} = \Delta m - m_{{}^{140}_{54}\text{Xe}} - m_{{}^1_0\text{n}} + m_{{}^{235}_{92}\text{U}}$$

$$\Rightarrow m_{{}^{94}_{38}\text{X}} = 93.953 u$$

III- Abundance of uranium isotopes

$$\left\{ \begin{array}{l} \bar{M}_U = \frac{m_{{}^{235}_{92}\text{U}} \cdot X_1 + m_{{}^{238}_{92}\text{U}} \cdot X_2}{100} \\ X_1\% + X_2\% = 100\% \end{array} \right.$$

- Natural abundance of ${}^{235}_{92}\text{U}$: $X_2\% = 0.38\%$
- Natural abundance of ${}^{238}_{92}\text{U}$: $X_1\% = 99.62\%$

Exercise 2:

I-

1- Transition corresponding to the given frequency

The Paschen series corresponds to transitions: $n_2=? \rightarrow n_1=3$

$$\nu = c \cdot R_H \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \quad n_2 > n_1$$

$$23.36 \times 10^{13} = 3 \times 10^8 \times 1.1 \cdot 10^7 \times \left(\frac{1}{3^2} - \frac{1}{n_2^2} \right)$$

$$\Rightarrow n_2^2 = \frac{1}{0.0401} = 24.94$$

$$\Rightarrow n_2 \approx 5$$

2-Energy corresponding to this transition:

Method 1: Using Planck's relation

$$E_{\text{ph}} = \Delta E = h \nu = (6.62 \times 10^{-34}) \cdot (23.36 \times 10^{13}) = 1.55 \times 10^{-19} \text{ J}$$

Method 2: Using energy levels of hydrogen

$$E_{ph} = |\Delta E| = |E_f - E_i| = |E_3 - E_5|$$

$$\Delta E = = \left| \frac{-13.6}{9} - \frac{-13.6}{25} \right| = 0.97 \text{ eV} \Rightarrow = 1.55 \times 10^{-19} \text{ J}$$

3-

For the Balmer series:

The second line corresponds to the transition $n_i=4 \rightarrow n_f=2$

$$\frac{1}{\lambda_1} = R_H \left(\frac{1}{4} - \frac{1}{16} \right) = R_H \left(\frac{3}{16} \right)$$

$$\Rightarrow \frac{1}{\lambda_1} = \frac{3 \cdot R_H}{16}$$

For the Paschen series:

The **third line** corresponds to the transition $n_i=6 \rightarrow n_f=3$

$$\frac{1}{\lambda_2} = R_H \left(\frac{1}{9} - \frac{1}{36} \right) = R_H \left(\frac{3}{36} \right)$$

$$\Rightarrow \frac{1}{\lambda_2} = \frac{R_H}{12}$$

$$\frac{\frac{1}{\lambda_1}}{\frac{1}{\lambda_2}} = \frac{\frac{3 \cdot R_H}{16}}{\frac{R_H}{12}}$$

$$\Rightarrow \lambda_2 = \frac{9}{4} \lambda_1 = \frac{9}{4} \cdot 486 = 1093.5 \text{ nm}$$

II-

1-Determination of Z for the hydrogen-like ion

$$\nu_1 = c \cdot Z^2 \cdot R_H \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = 3 \times 10^8 \times Z^2 \times 1.1 \cdot 10^7 \times \left(\frac{1}{9} - \frac{1}{25} \right)$$

$$Z^2 = \frac{210.29 \times 10^{13}}{3 \times 10^8 \times 1.1 \cdot 10^7 \times \left(\frac{1}{9} - \frac{1}{25} \right)} = 9 \Rightarrow Z = 3$$

2- Energy required to ionize the ion from $n=5$

$$E_i = \Delta E = E_\infty - E_5 = \frac{9 \times (-13.6)}{\infty^2} - \frac{9 \times (-13.6)}{25} = 4.896 \text{ eV}$$

Exercise 3:

1-

Element	configuration	Period	Group	Column
${}_{16}\text{S}$	$10[\text{Ne}] 3s^2 3p^4$	3	VI _A	16
${}_{48}\text{Cd}$	$36[\text{Kr}] 5s^2 4d^{10}$	5	II _B	12
${}_{37}\text{Rb}$	$36[\text{Kr}] 5s^1$	5	I _A	1

2-Order of atomic radii

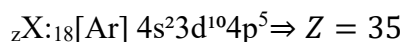
The atomic radius decreases as the atomic number increases across a single period from left to right.

$$r_{17\text{Cl}} < r_{16\text{S}} < r_{15\text{P}}$$

The explanation for this: is that with an increase in the atomic number, the positive charges (number of protons) in the nucleus gradually increase while the principal energy levels within the period remain constant. As a result, the attractive force between the nucleus and the valence electrons increases, leading to a decrease in the atomic radius.

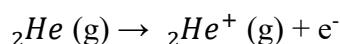
3-Identification of element X

X has 5 electrons in the subshell defined by $\left\{ \begin{array}{l} \ell = 1 \Rightarrow p \text{ subshell} \\ n = 4 \Rightarrow \text{the subshell is } 4p \\ \text{and the noble gas preceding } X \end{array} \right.$



$7 > 4 \Rightarrow X$ is a **non-metal**

4- First ionization energy of ${}_2\text{He}$ using Slater's rules



$$E_{i_1} = E_{{}_2\text{He}^+} - E_{{}_2\text{He}}$$

$${}_2\text{He}: 1s^2 \quad E_{{}_2\text{He}} = 2E_{1s}$$

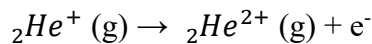
$${}_2\text{He}^+: 1s^1 \quad E_{{}_2\text{He}^+} = E'_{1s}$$

$$E_{i_1} = E_{{}_2\text{He}^+} - E_{{}_2\text{He}} = 2E_{1s} - E'_{1s}$$

$$E_{i_1} = 2 \frac{Z^{*2} E_H}{n^{*2}} - \frac{Z'^{*2} E_H}{n^{*2}} = 2 \frac{(2 - 0.31 \times 1)^2 \times (-13.6)}{1^2} - \frac{(2)^2 \times (-13.6)}{1^2}$$

$$E_{i_1} = 23.285 \text{ eV}$$

- Second ionization energy



$$E_{i_2} = E_{{}_2\text{He}^{2+}} - E_{{}_2\text{He}^+}$$

$${}_2\text{He}^{2+}: 1s^0 \quad E_{{}_2\text{He}^{2+}} = 0 \text{ eV}$$

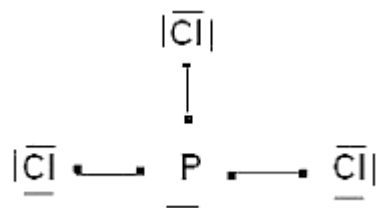
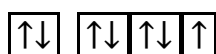
$${}_2\text{He}^+: 1s^1 \quad E_{{}_2\text{He}^+} = E'_{1s}$$

$$E_{i_2} = E_{{}_2\text{He}^{2+}} - E_{{}_2\text{He}^+} = -E'_{1s}$$

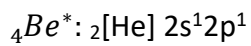
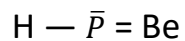
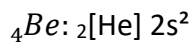
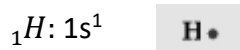
$$E_{i_2} = -\frac{(2)^2 \times (-13.6)}{1^2} = 54.4 \text{ eV}$$

Exercise 4: (2 pts)

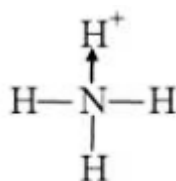
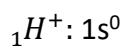
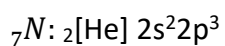
1- Lewis structures of PCl_3



Lewis structures of HPBe



Lewis structures of NH_4^+



Or

